## experiment Surface plasmons in silver films-a novel undergraduate

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necessary to produce the required thin silver films. are calculated. Only a modest vacuum of  $\sim 10^{-3}$  Torr is minimum in the reflectivity results from the absorption of sponding to the excitation of the surface plasmon. The sharp minimum in the reflected light is observed, corre-Light (p-polarized) from a He-Ne laser is incident through evaporated on the hypotenuse face of a right glass prism ory for a senior level undergraduate investigation of surface the reflectivity due to the excitation of this normal mode film. The dispersion relation for the surface plasmon and the resonantly enhanced surface plasmon mode in the silver degrees greater than the critical angle for total reflection, a the prism on the metal film. At an angle of incidence a few plasmons in silver films. An  $\sim 500$ -A-thick silver film is current interest. We describe a simple experiment and the Surface plasmon phenomena are a topic of considerable

#### INTRODUCTION

on a semi-infinite dielectric bounded by vacuum is given by ponentially attenuated in the normal direction in both the metal and air. The wave vector,  $k_x$ , of a surface plasmon parallel to the interface (along the x direction) and are exelectromagnetic waves, traveling along the interface of be a metal and the other to be air. The waves propagate two different media. We will assume one of the media to Surface plasma waves are transverse magnetic (TM)

$$k_x = \frac{\omega}{c} \left( \frac{\epsilon}{\epsilon + 1} \right)^{1/2}, \tag{1}$$

from Eq. (1) that  $k_x$  is greater than the wave vector of an than -1 in the visible region of the spectrum, and we see at the angular frequency  $\omega$ . For most metals  $\epsilon(\omega)$  is less mon waves may be excited only with evanescent waves and are therefore classified as nonradiative. Collective bselectromagnetic wave in air at the same  $\omega$ . Surface plaswhere  $\epsilon$  is the complex dielectric function of the medium

> may be described in terms of these waves.1 cillations in the electron density at the surface of a metal

ing the method of attenuated total reflection where the evanscent wave is either coupled from the prism into the these waves as surface polaritons, corresponding to those solutions of Maxwell's equations which are subject to the mon mode in silver films was first recognized by Otto usas solutions of Maxwell's equations since Sommerfeld of the surface plasmon mode in silver films enhances the the prism into a thin metal film.3 Agarwal has described metal through a thin air spacing, or directly coupled from ever, he did not attribute this phenomenon to a surface production of optical second-harmonic generation.5 Recently, the present authors have shown that excitation Ewald-Oseen extinction theorem with no incident field. plasmon resonance.2 The excitation of the surface plasinternal reflection was first observed by Turbadar; how-The decrease in reflectivity from aluminum films in total Nonradiative surface plasma waves have been known

evaporated at pressures as high as 10-3 Torr. We coning the observed minimum in reflectivity. In the final secsurface plasmons in other metals and the dispersion of the clude by suggesting extensions of this experiment to study tion, we describe the experimental apparatus and discuss citation of this mode by the method of attenuated total resion relation given by Eq. (1). Next, we describe the exdescribe the surface plasmon mode and derive the dispertypical results that can be obtained from silver films hanced internal optical fields in the metal film for producflection. Emphasis is placed on the absorption of the en-We divide our discussion into three sections. First, we

# SURFACE PLASMON DISPERSION

will assume  $\epsilon_2 \equiv 0$  for the purpose of discussing ideal surface plasmon dispersion. The space for z < 0 is assumed to be air of dielectric constant unity. The essential cy.6 The imaginary part of the dielectric constant describes the optical absorption processes in the metal. We  $\epsilon_1 = 1 - \omega_p^2/\omega^2$ , where  $\omega_p$  is the bulk plasmon frequendielectric constant for a free electron metal is given by dielectric function  $\epsilon = \epsilon_1 + i\epsilon_2$ . The real part of the We now derive a dispersion relation that will relate the propagation vector of a surface wave traveling along the assumed to be monochromatic plane waves: the space z > 0 to be filled with a metal with complex wave on each side of the boundary. The electric fields are assumption is to postulate the existence of only a single surface of a metal to its angular frequency. We consider

$$\mathbf{E}(x, z, t) = \mathbf{E} \exp[i(\omega t - k_x x - k_z z)]. \tag{2}$$

real numbers and uses the wave equation to determine the frequency of the propagating wave. Instead of this procedure, we assume that  $\omega$  is given and  $k_{\infty}$  is a real number gation in an infinite solid, one takes  $k_x$  and  $k_z$  to be given may now be written. Normally, in studying wave propa-The complete wave equation for this wave in each region

> waves in either the metal or air. We assume  $\omega$  and  $k_x$ wave equation can be written have values such that in the metal the solution of the the conditions under which there are no propagating to be determined.7 For surface waves we are interested in

$$k_z = -i(k_x^2 - \epsilon\omega^2/c^2)^{1/2}$$
 (3a)

and in air

$$k_z = +i(k_x^2 - \omega^2/c^2)^{1/2}.$$
 (3b)

tal internal reflection. in the visible region of the spectrum where  $\omega < \omega_p$ ; in air this condition is satisfied only for evanescent waves in tothe boundary. In metals this condition is easily satisfied metal and dielectric describe exponential decay normal to The signs are chosen so that the electric fields in the

of the fields, we have tinuity of the tangential component of E and transversality case of interest is  $E_{\nu} = 0$ , p-polarization. Now, using cons-polarization, no plasma mode solution is found. The lel or perpendicular to the plane of incidence defined by  $k_x$  and the z axis. For the case in which  $E_x = E_z = 0$ , The boundary conditions at the plane z=0 are the standard ones; continuity of the tangential component of E and H and of the normal component of D and B. We is equal to H. The two transverse modes can be classified assume the magnetic permeability is equal to unity, and B by their polarizations, namely, with electric field E paral-

$$k_{\varepsilon} E_{\varepsilon} \Big|_{\varepsilon=0+} = k_{\varepsilon} E_{\varepsilon} \Big|_{\varepsilon=0-}.$$
 (4)

ponent of D gives Combining the above with continuity of the normal com-

$$\frac{k_{x}}{k_{x}}\Big|_{s=0^{+}} = \frac{k_{x}}{k_{x}}\Big|_{s=0^{-}}.$$
(5)

Substitution from Eqs. (3a) and (3b) allows the above condition to be rewritten as the dispersion relation given

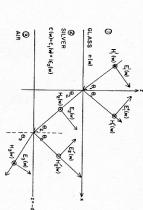
### SURFACE PLASMON EXCITATION

and reflected propagating wave of the form plane waves. In the glass medium we have an incident geometry is shown in Fig. 1. We assume the electric field angle of incidence greater than the critical angle for total metal film at the hypotenuse face of the prism and at an tromagnetic wave in a glass prism is incident on a thin plasmon mode to the exciting incident radiation. An elecvectors are p-polarized and described by monochromatic internal reflection. The attenuated total reflection In this section we relate the amplitude of the surface

$$\mathbf{E}_{\text{incident}} = \mathbf{E}_i^{\ i} \exp[i(\omega/c)\pi(x\sin\theta_1 - z\cos\theta_1)] \quad (6a)$$

and

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tween a glass prism and air. Fig. 1. Attenuated total reflection geometry for a thin metal film be-

$$\mathbf{E}_{\text{reflected}} = \mathbf{E}_{1}^{r} \exp[i(\omega/c)n(x\sin\theta_{1} + z\cos\theta_{1})].$$
 (6b)

waves: standing wave superposition of two exponentially damped In the thin metal film we write the total electric field as a

$$\begin{split} \mathbf{E}_{\text{metal}} &= \mathbf{E}_{2} \exp[i(\omega/c)nx \sin\theta_{1}] \exp(\hbar z) \\ &+ \mathbf{E}_{2}' \exp[i(\omega/c)nx \sin\theta_{1}] \exp(-kz). \end{split} \tag{6c}$$

The transmitted wave in the vacuum is assumed evanes

$$\mathbf{E}_{\text{transmitted}} = \mathbf{E}_{\tilde{s}} \exp[i(\omega/c)nx \sin\theta_i]$$

$$\times \exp\left[(\omega/c)(n^2\sin^2\theta_i - 1)^{1/2}z\right]. (6d)$$

Here k is the absorption coefficient at nonnormal incidence, which by comparison with Eqs. (2) and (3a) is written for the geometry of Fig. 1 as

$$k = -i(\omega/c)(\epsilon - n^2 \sin^2 \theta_1)^{1/2},$$
 (7)

as before, n is the index of refraction of the glass, and  $\theta_1$  is the angle of incidence. The x dependence of all the waves follows from Snell's law. where  $\epsilon$  is the complex dielectric coefficient of the metal

of E and H at the z = 0 and z = -d boundaries gives be related to the incident amplitude  $E_1$ , through the boundof the fields in the metal at z = 0 to be the required four equations. We thus find the amplitude ary conditions. Continuity of the tangential components The four unknown amplitudes  $E_1^r$ ,  $E_2$ ,  $E_2^r$ , and  $E_3$  can

$$E_2 = E_1^{i} \frac{t_{12}}{1 + r_{12}r_{23} \exp(-2kd)}$$
 (8a)

and

$$E_{2}' = E_{1}' \frac{t_{12}r_{23} \exp(-2kd)}{1 + r_{12}r_{23} \exp(-2kd)}.$$
 (8b)

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The Fresnel reflection and transmission amplitude factors, with the 12 and 23 subscripts for the glass-metal and metal-air boundaries, respectively, are given by

$$t_{12} = \frac{2n\cos\theta_1}{\epsilon^{1/2}\cos\theta_1 + n\cos\theta_2},\tag{9a}$$

$$r_{12} = \frac{e^{1/2}\cos\theta_1 - n\cos\theta_2}{e^{1/2}\cos\theta_1 + n\cos\theta_2},$$
 (9b)

$$r_{23} = \frac{\cos \theta_2 - \epsilon^{1/2} \cos \theta_3}{\cos \theta_2 + \epsilon^{1/2} \cos \theta_3}.$$
 (9c)

and

The angles  $\theta_2$  and  $\theta_3$  in the metal and air, respectively, are defined by

$$\cos \theta_2 = (1 - n^2 \sin^2 \theta_1 / \epsilon)^{1/2}$$
 (10a)

and

$$\cos\theta_3 = (1 - n^2 \cdot \sin^2\theta_1)^{1/2}.$$
 (10b)

optical power to the incident optical power to be given by nential decay of the fields in the metal and air media. The complex nature of these angles reflects the real expo-We now solve for  $E_1$  and find the ratio of the reflected

$$R = \left| \frac{r_{12} + r_{23} \exp(-2kd)}{1 + r_{12}r_{23} \exp(-2kd)} \right|^{2}.$$
 (11)

be rewritten as The critical factor in the above formula is  $r_{23}$ , which may

$$\gamma_{23} = \frac{(n^2 \sin^2 \theta_1 - \epsilon)^{1/2} - \epsilon (n^2 \sin^2 \theta_1 - 1)^{1/2}}{(n^2 \sin^2 \theta_1 - \epsilon)^{1/2} + \epsilon (n^2 \sin^2 \theta_1 - 1)^{1/2}}.$$
 (12)

vanishes at the plasmon angle  $\theta_p$  given by For an ideal free electron plasma, the denominator of  $r_{23}$ 

$$n\sin\theta_{p} = [\epsilon/(\epsilon+1)]^{1/2},\tag{13}$$

given by Eq. (1). The divergence of  $r_{23}$  at the surface plasmon resonance was recognized by Cardona<sup>9</sup> and can consistent with the surface plasmon mode discussed preboundary to the metal-glass boundary. This description is has a simple exponential spatial decay from the metal-air when  $\theta_1 = \theta_p$  then  $E_2 \equiv 0$  and the only field in the metal gent factors, is to recognize directly from Eq. terface. A more direct interpretation, without any diverfield to a zero-amplitude incident field at the metal-air inbe described as the ratio of a finite-amplitude reflected which is also the condition for the surface plasmon mode (8a) that

viously and the surface polariton modes of Agarwal. 

The effect of the surface plasmon resonance on the

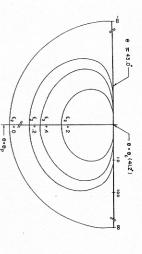
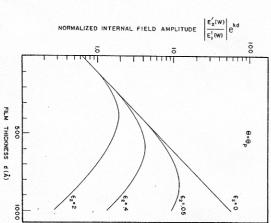


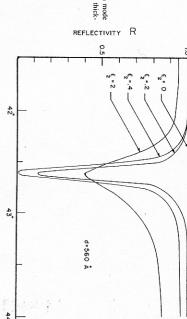
Fig. 2. Polar plot of the complex Fresnel reflection factor,  $r_{23}$ , at the silver-air interface for angles of incidence around the plasmon angle. The amplitude scale is logarithmic.

we have  $r_{22} \simeq 1$ , but at the plasmon angle  $r_{23} \simeq -i2\epsilon_1/\epsilon_2$ , and beyond this angle  $r_{23}$  rapidly approaches  $\simeq -1$ . The is plotted in Fig. 2 with a logarithmic amplitude scale. At the critical angle for total internal reflection ( $n \sin \theta_c = 1$ ), real part of Eq. (13), but r<sub>23</sub> now assumes a large neganance may still be observed through enhanced harmonic generation. <sup>6</sup>] The plasmon and  $a : -\frac{1}{2}$ amplitude and phase of  $r_{23}$  are a sensitive function of the tive imaginary value. The amplitude and phase of  $r_{23}$  in gles of incidence including the surface plasmon resonance; tivity calculated from Eq. (11) remains unity for all anlinear reflectivity can be observed only for the case of nonzero absorption given by  $\epsilon_2 \neq 0$ . [If  $\epsilon_2 = 0$ , the reflecthe complex plane as a function of the angle of incidence



evaluated at the silver-air interface versus film thickness Fig. 3. Normalized amplitude of the surface plasmon mode electric field

ness and variable absorption constant versus angle of incidence for fixed film thick-Fig. 4. Reflectance of the surface plasmon mode



angle of incidence in this region.

ANGLE OF INCIDENCE 0

is nonzero, although it is still several orders of magnitude son the normalized amplitude of the other field in the metal film for zero absorption is identically zero, as preamplitude reaches a maximum, which may be an order of magnitude larger than the incident field. By comparismaller than the surface plasmon mode field shown in viously discussed; however, for finite absorption this field film; however, for nonzero absorption this internal field this field increases exponentially with the thickness of the scale is logarithmic. For zero absorption the amplitude of film thickness for several values of  $\epsilon_2$ . Note the amplitude evaluated at the metal-air boundary as a function of metal surface plasmon mode electric field at the plasmon angle In Fig. 3 we display the normalized amplitude of the

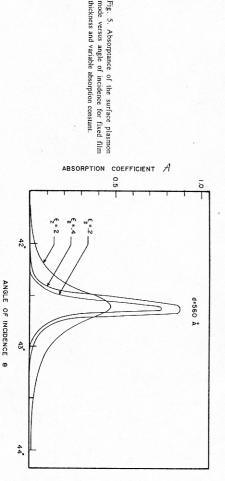
Fig. 3.

The quantity of experimental interest is the reflectance which is shown in Fig. 4 as a function of the angle of incidence for a fixed film thickness. Again for zero absorption the reflectivity is unity but decreases sharply near

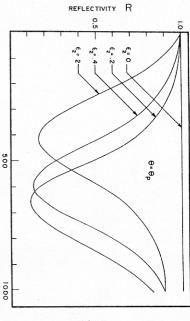
the surface plasmon, given by metal film. Integrating the power absorption density over enhanced internal fields throughout the volume of the tivity minimum is no longer sharp. The effect of damping on the surface plasmon resonance has been discussed by the irradiated volume of the film and normalizing by the several authors. 10 The reflectivity minimum at the plascreases with absorption. For large values of absorption, incident power, we have the enhanced absorptance due to mon resonance is due to the increased absorption of the the plasmon resonance is heavily damped and the reflecthat the angular half-width of these resonant curves in the plasmon resonance as the absorption increases. Note

$$\mathcal{A} = \frac{\epsilon_2 \omega \left[ \exp(2kd) - 1 \right] \cos \theta_2}{nc2k \cos \theta_1} \left| \frac{E_2'}{E_1'} \right|^2. \tag{14}$$

The above quantity is plotted in Fig. 5. Clearly, the maxima in the absorptance match the minima in the reflec-



thickness and variable absorption constant.



at the plasmon angle versus film thickness for variable absorption constant. Fig. 6. Reflectance of the surface plasmon mode

angle as a function of film thickness in order to estimate the optimum film thickness in the following section. tance. In Fig. 6 we show the reflectance at the plasmon

FILM THICKNESS d(A)

#### EXPERIMENT AND RESULTS

current was turned off and the pressure inside the bell jar process begun. After a few minutes of evaporation, the silver to slowly melt into a small ball at the bottom of the caused the filament to gradually glow red hot and the block any impurities that might boil off while the silver metal shutter, magnetically coupled to the outside of the reagent grade methanol and rinsed with distilled water. A sults, and make suggestions for further experiments. Our evaporating thin silver films, discuss the experimental rewas returned to atmospheric. filament. The shutter was then opened and the coating in Fig. 7. A current of 4-8 A supplied by a Variac was initially heated. A sketch of this apparatus is shown bell jar, was placed between the silver and the prism to to the electrodes. Before the prism was placed at the botwas placed at the bottom of the coil which was attached basket was made from tungsten or molybdenum wire. A a No. 8 rubber stopper at its top through which the two apparatus which produced a vacuum of 10-3 Torr contom of the bell jar, the hypotenuse face was cleaned with 1.5-cm length of 99.999% silver wire<sup>11</sup> (1-mm diameter) electrodes entered the vacuum chamber. A coiled filament Vector 75 rotary roughing pump and a 6-in. bell jar with sisted of an Edwards 3-in. diffusion pump connected to a In this section we describe a simple apparatus for

on a white piece of paper. At the critical angle for total of incidence by a Polaroid sheet was incident on the tensity from the laser spot on the back silver-air surface prism, and the reflected beam could initially be observed spectrometer. The prism was then removed from the evaporator and A simultaneous increase in the scattered-light inon a suitable rotary platform or a student grade first to decrease sharply and then to increase A He-Ne laser beam polarized in the plane

> this experiment was comparable to the extinction obtained sured with a voltmeter, the results shown in Fig. 8 were obtained. The minimum in reflected intensity observed in with a RCA 1P28 photomultiplier whose output was meawas also observed. When the reflected light was detected with crossed polarizers.

greater than 800 Å thick will produce shallow reflectivity Fig. 6, we see that films either less than 300 Å thick or perience is coating the correct film thickness. Referring to The only experimental technique requiring a little ex-

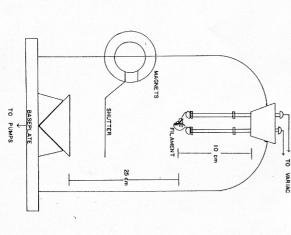
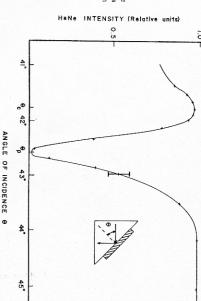


Fig. 7. Sketch of simple evaporator apparatus. Prism with hypotenuse face up rests on the base plate.

at the He-Ne laser wavelength 6328 A. silver film 560 Å thick on a crown glass prism plasmon mode versus angle of incidence in a Fig. 8. Experimental reflectance of the surface



proximately 1% at 6328 A. in this experiment, the transmission of the slide was aptransmission of the coated slide. For the 560-A film used surface in the evaporator and measuring the optical mined by placing a microscope slide adjacent to the prism desired effect is achieved. Film thickness may be deterples of varying thickness may be easily prepared until the Since this process requires only a few minutes, new sambe recleaned and the evaporation process repeated again. face plasmon resonance is not observed, the prism should prism should be visible through the metal film. If the surappear semitransparent; however, the apex edge of the thick a film will appear opaque while too thin a film will minima. When viewed from the hypotenuse face, 100

evaporated under high vacuum (10-9 Torr) and remain in period of several weeks. Although the films should be observable over a large range of  $\epsilon_2$ . the qualitative features of the reflectivity minimum should properties of the silver film are sensitive to the conditions of film preparation (especially at our vacuum pressure of are not necessary for the qualitative observation of surface vacuum during the experiment, such stringent conditions played in Fig. 8 were repeatable with the same film mainthe reflectance to this parameter. We see from Fig. 4 that 10-3 Torr) and to the growth of silver sulfide layers on computer. The complex dielectric constant of the silver film<sup>12</sup> was  $\epsilon = -18.3 + i0.4$  at the He-Ne laser Figs. 2-6 were performed on a PDP-11 time-sharing take on a wide range of values to test the sensitivity of the film in air 13; therefore, the value of  $\epsilon_2$  was allowed to crown glass prism was taken to be n = 1.52. The optical wavelength (6328 A), and the index of refraction of the The numerical calculations for the curves presented in the ambient laboratory environment over a The results disbe

the dispersion relation for the surface plasmon. This curve source, which was chosen solely for its experimental confunction of wavelength, one can experimentally determine the angle at which the reflectivity minimum occurs as a venience, with a collimated monochromator. By measuring There are several interesting extensions of this experi-One experiment is to replace the He-Ne laser

> film, Turbadar<sup>2</sup> gives a thickness of 125 Å at a wavelength of 5500 Å. The dispersion of surface plasmons in gold films has been studied by Barker. <sup>15</sup> The surface plasmon resonance in many metals by use of the technique we have described here. opportunity exists to make original observations of the smaller film thicknesses than in silver. For an aluminum als. 14 The sharpest reflectivity minima will now occur for is the magnitude of the ratio  $\epsilon_1/\epsilon_2$ . For silver in the near infrared, this ratio is larger than that of the other metestimating the strength of the surface plasmon resonance aluminum, gold, and copper. The relevant parameter for metals which can be easily evaporated, for example, the surface plasmon. 10 Another experiment is to use other termined dispersion curve is a result of the damping of bending in the near ultraviolet of this experimentally demay then be compared with Eq. (1). The observed back

of the effect of the surface plasmon mode on the reflectivture demonstration for a more general audience dents, but should also provide a dramatic effect in a leconly provide a stimulus in the laboratory for physics studramatic change in reflectivity of a silver film should not films may be prepared with a modest apparatus. The ity of thin metal films and have demonstrated how such In conclusion, we have given a theoretical description

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